



#### User-friendly Probabilistic Decision Logic Modeling

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#### Aim of presentation

- Highlight role of uncertainty in decision making
- Show that DMN is a great foundation for user-friendly probabilistic modeling



### Introduction

- Simon Vandevelde
- PhD student @ CS, KU Leuven university, Belgium
- Research on symbolic Al
- Specific focus on user-friendliness
  - How do we make knowledge-based systems more accessible?
- DMN is obviously of interest



### Introduction





### Introduction





• DMN from a more theoretical viewpoint





• DMN from a more theoretical viewpoint – but still practically applied





- DMN from a more theoretical viewpoint but still practically applied
- **DMN-IDP**<sup>1</sup>: Do more with DMN



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- DMN from a more theoretical viewpoint but still practically applied
- **cDMN**<sup>2</sup>: Extend DMN with constraints

| Doctor works max. 1 shift per day |            |   |                            |
|-----------------------------------|------------|---|----------------------------|
| E*                                | Doctor Day |   | nb shifts of Doctor on Day |
| 1                                 | -          | 9 | $\leq 1$                   |

| Group size     |       |                 |
|----------------|-------|-----------------|
| $\mathrm{E}^*$ | Group | number in Group |
| 1              |       | [16, 19]        |



DecisionCAMP 2020, "cDMN: Combining DMN with constraint reasoning"

- DMN from a more theoretical viewpoint but still practically applied
- How to properly handle unknown values?

| Salutation |        |         |       |
|------------|--------|---------|-------|
| U          | Gender | MStatus | Salut |
| 1          | Male   | -       | Mr    |
| 2          | Female | Married | Mrs   |
| 3          | Female | Single  | Ms    |

(c) Salutation decision table

- DMN from a more theoretical viewpoint but still practically applied
- How to properly handle unknown values?
- Undefined is not unknown!

| Sal | Salutation |         |       |
|-----|------------|---------|-------|
| υ   | Gender     | MStatus | Salut |
| 1   | Male       | -       | Mr    |
| 2   | Female     | Married | Mrs   |
| 3   | Female     | Single  | Ms    |

(c) Salutation decision table

- DMN from a more theoretical viewpoint but still practically applied
- **pDMN:** how to elegantly incorporate probabilities?



# Uncertainties

- Life is inherently uncertain
  - Will it rain?

. . .

- How much traffic will there be?
- Will the medicine be effective?

• Massive shift to learning/predicting from data: these are all (un)certainties!



### Probabilities can be "forced" into DMN

| Um | ıbrella        |          |
|----|----------------|----------|
| U  | Rain           | Umbrella |
| 1  | Certainly      | Yes      |
| 2  | Maybe          | Yes      |
| 3  | Definitely Not | No       |



# Probabilities can be "forced" into DMN

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| 2  | Maybe          | Yes      |
| 3  | Definitely Not | No       |

| Um | ıbrella             |          |
|----|---------------------|----------|
| U  | Probability of Rain | Umbrella |
| 1  | > 30                | Yes      |
| 2  | $\leq 30$           | No       |



# Probabilities can be "forced" into DMN

- Very rigid
- Table "hides" the probability
- You cannot express probability on input value
  - E.g., a dice has a chance of 1/6 to be 1, 2, ...

| Um | ıbrella        |          |
|----|----------------|----------|
| U  | Rain           | Umbrella |
| 1  | Certainly      | Yes      |
| 2  | Maybe          | Yes      |
| 3  | Definitely Not | No       |

| Um | brella              |          |
|----|---------------------|----------|
| U  | Probability of Rain | Umbrella |
| 1  | > 30                | Yes      |
| 2  | $\leq 30$           | No       |



#### Goal

- Extend DMN with probabilities:
  - Elegantly, in DMN-like way
  - Presence of probability should be clear
  - Reason on them throughout entire model!

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• Build an inference engine for this notation

# pDMN

- DMN extension for probabilistic logic
- DMN is a great foundation!
  - User-friendly, readable
  - Table-based format, very intuitive

Note: we do advocate for adding probabilities to official DMN standard, but want to point out that it forms an excellent foundation for a probabilistic notation.



# pDMN: glossary

- Symbols can have arity n
- i.e., functions and predicates are possible
- Must be declared in glossary

|           |                   | Predicate    |            |           |
|-----------|-------------------|--------------|------------|-----------|
| Туре      |                   | Name         | Fund       | tion      |
| Name      | Elements          | burglary     | Nama       | Tuno      |
| Person    | john, mary        | alarm        |            | Iype      |
| Intensity | heavy, mild, none | Person calls | eartnquake | Intensity |
|           | ••••              | anycalls     |            |           |



• pDMN extends decision tables with three new concepts



- pDMN extends decision tables with three new concepts
  - Probabilities



- pDMN extends decision tables with three new concepts
  - Probabilities

| Burglary |          |
|----------|----------|
| U        | burglary |
|          | Yes      |
| 1        | 0.7      |



- pDMN extends decision tables with three new concepts
  - Probabilities

| Burglary |          |
|----------|----------|
| U        | burglary |
|          | Yes      |
| 1        | 0.7      |

| Ala | Alarm    |       |      |  |  |  |
|-----|----------|-------|------|--|--|--|
| U   | burglary | alarm |      |  |  |  |
|     |          |       | Yes  |  |  |  |
| 1   | Yes      | heavy | 0.9  |  |  |  |
| 2   | Yes      | mild  | 0.85 |  |  |  |
| 3   | Yes      | none  | 0.8  |  |  |  |
| 4   | No       | mild  | 0.1  |  |  |  |
| 5   | No       | heavy | 0.3  |  |  |  |



- pDMN extends decision tables with three new concepts
  - Probabilities
  - Ch(oice) hit policy



- pDMN extends decision tables with three new concepts
  - Probabilities
  - Ch(oice) hit policy

| Earthquake |            |      |      |  |
|------------|------------|------|------|--|
| Ch         | earthquake |      |      |  |
|            | heavy      | mild | none |  |
| 1          | 0.01       | 0.19 | 0.8  |  |



- pDMN extends decision tables with three new concepts
  - Probabilities
  - Ch(oice) hit policy

| Earthquake |            |      |      |  |
|------------|------------|------|------|--|
| Ch         | earthquake |      |      |  |
|            | heavy      | mild | none |  |
| 1          | 0.01       | 0.19 | 0.8  |  |

| Thro | wing Dice |           |     |       |      |      |     |
|------|-----------|-----------|-----|-------|------|------|-----|
| Ch   | biased    | die value |     |       |      |      |     |
|      |           | one       | two | three | four | five | six |
| 1    | No        | 1/6       | 1/6 | 1/6   | 1/6  | 1/6  | 1/6 |
| 2    | Yes       | 0.1       | 0.1 | 0.1   | 0.1  | 0.1  | 0.5 |



- pDMN extends decision tables with three new concepts
  - Probabilities
  - Ch(oice) hit policy
  - Quantification (for every)



- pDMN extends decision tables with three new concepts
  - Probabilities
  - Ch(oice) hit policy
  - Quantification (for every)

| Cal | ls    |         |
|-----|-------|---------|
| U   | alarm | X calls |
|     |       | Yes     |
| 1   | Yes   | 0.8     |
| 2   | No    | 0.1     |



- pDMN extends decision tables with three new concepts
  - Probabilities
  - Ch(oice) hit policy
  - Quantification (for every)

| Cal | ls    |         |
|-----|-------|---------|
| U   | alarm | X calls |
|     |       | Yes     |
| 1   | Yes   | 0.8     |
| 2   | No    | 0.1     |

| any | calls   |          |
|-----|---------|----------|
| U   | X calls | anycalls |
| 1   | Yes     | Yes      |



# pDMN: query

- We want to calculate probability of a symbol
- Query table informs solver of symbols





|           |                   | Predicate    |             |           |
|-----------|-------------------|--------------|-------------|-----------|
| Туре      |                   | Name         | Funct       | tion      |
| Name      | Elements          | burglary     | Name        |           |
| Person    | john, mary        | alarm        | earthquake  | Intensity |
| Intensity | heavy, mild, none | Person calls | Cartilquake | intensity |
|           |                   | anycalls     |             |           |

| Burglary | Farthquake | 1     |            |      | Cal | ls    |         |
|----------|------------|-------|------------|------|-----|-------|---------|
| Burgiary | Laruquake  |       | .1 1       |      | U   | alarm | X calls |
| U burgla | y    Ch    | ea    | earthquake |      |     |       | Ves     |
| Yes      |            | heavy | mild       | none | 1   |       | 105     |
| 1 07     | 1          | 0.01  | 0.10       | 0.8  |     | Yes   | 0.8     |
| 1 0.7    |            | 0.01  | 0.19       | 0.0  | 2   | No    | 0.1     |

| Ala | rm       |            | ]     |   |         |          |         |
|-----|----------|------------|-------|---|---------|----------|---------|
| U   | burglary | earthquake | alarm | ] |         |          |         |
|     |          |            | Yes   | ] | calls   | 1        | Query   |
| 1   | Yes      | heavy      | 0.9   |   | V collo | anvoalla | Vaella  |
| 2   | Yes      | mild       | 0.85  |   |         |          | A calls |
| 3   | Yes      | none       | 0.8   |   | ies     | ies      | anycans |
| 4   | No       | mild       | 0.1   | 1 |         |          |         |
| 5   | No       | heavy      | 0.3   | 1 |         |          |         |



|           |                   | Predicate    |             |           |
|-----------|-------------------|--------------|-------------|-----------|
|           | Туре              | Name         | Funct       | tion      |
| Name      | Elements          | burglary     | Nama        | Type      |
| Person    | john, mary        | alarm        | aarthquaka  | Intensity |
| Intensity | heavy, mild, none | Person calls | Cartilyuake | Intensity |
|           |                   | anycalls     |             |           |

| Burglary | 1        | Farthquake | 1          |      |      | Cal | ls    |         |
|----------|----------|------------|------------|------|------|-----|-------|---------|
| Durgiary | 1 1      |            |            |      |      | U   | alarm | X calls |
| 0        | burglary | Ch         | earthquake |      |      |     |       | Ves     |
|          | Yes      |            | heavy      | mild | none | 1   | Vac   | 0.8     |
| 1        | 0.7      | 1          | 0.01       | 0.19 | 0.8  | 1   | 165   | 0.0     |
|          | 0.7      |            | 0.01       | 0.17 | 0.0  | 2   | No    | 0.1     |

person\_calls(mary): 0.45916, person\_calls(john): 0.45916, anycalls: 0.550992, }

| Ala            | rm       |            |       |   |         |          |          |
|----------------|----------|------------|-------|---|---------|----------|----------|
| U              | burglary | earthquake | alarm | ] |         |          |          |
|                |          |            | Yes   | ] | calls   | ]        | Query    |
| 1              | Yes      | heavy      | 0.9   |   |         | 11       | Vully    |
| $\overline{2}$ | Ves      | mild       | 0.85  |   | X calls | anycalls | X calls  |
|                | 105      | minu       | 0.05  | 1 | Yes     | Yes      | anvcalls |
| 3              | Yes      | none       | 0.8   |   |         |          |          |
| 4              | No       | mild       | 0.1   | 1 |         |          |          |
| 5              | No       | heavy      | 0.3   | ] |         |          |          |



- Someone came in contact with infected person
- You want to assess if they had high-risk contact



- Someone came in contact with infected person
- You want to assess if they had high-risk contact

| Vaccine |              |      |      |
|---------|--------------|------|------|
| Ch      | vaccine of X |      |      |
|         | a            | b    | n    |
| 1       | 0.36         | 0.63 | 0.01 |



- Someone came in contact with infected person
- You want to assess if they had high-risk contact

| Vaccine |              |      |      |  |
|---------|--------------|------|------|--|
| Ch      | vaccine of X |      |      |  |
|         | a            | b    | n    |  |
| 1       | 0.36         | 0.63 | 0.01 |  |

| In | fection       |               |              |               |
|----|---------------|---------------|--------------|---------------|
| U  | X contacted Y | Y is infected | vaccine of X | X is infected |
|    |               |               |              | Yes           |
| 1  | Yes           | Yes           | n            | 0.8           |
| 2  | Yes           | Yes           | a            | 0.1           |
| 3  | Yes           | Yes           | b            | 0.2           |



- Someone came in contact with infected person
- You want to assess if they had high-risk contact

| Vaccine |              |      |      |  |
|---------|--------------|------|------|--|
| Ch      | vaccine of X |      |      |  |
|         | a            | b    | n    |  |
| 1       | 0.36         | 0.63 | 0.01 |  |

| Infe |               |               |              |                  |               |
|------|---------------|---------------|--------------|------------------|---------------|
| U    | X contacted Y | Y is infected | vaccine of X | contact distance | X is infected |
|      |               |               |              |                  | Yes           |
| 1    | Yes           | Yes           | n            | > 5              | 0.3           |
| 2    | Yes           | Yes           | а            | > 5              | 0.05          |
| 3    | Yes           | Yes           | b            | > 5              | 0.05          |
| 4    | Yes           | Yes           | n            | $\leq 5$         | 0.8           |
| 5    | Yes           | Yes           | a            | $\leq 5$         | 0.1           |
| 6    | Yes           | Yes           | b            | $\leq 5$         | 0.2           |







# pDMN engine

Uses ProbLog internally:

• pDMN tables are translated to ProbLog

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• ProbLog calculates the probabilities

# pDMN engine

Uses ProbLog internally:

- pDMN tables are translated to ProbLog
- ProbLog calculates the probabilities

```
% Vaccine
0.36::vaccine_of_Person(X, a);0.63::vaccine_of_Person(X, b);0.01::vaccine_of_Person(X, n) :- person(X).
```

% Infection

```
0.8::person_is_infected(X) :- person_contacted_Person(X, Y), person_is_infected(Y), vaccine_of_Person(X, n), person(X), person(Y).
0.1::person_is_infected(X) :- person_contacted_Person(X, Y), person_is_infected(Y), vaccine_of_Person(X, a), person(X), person(Y).
0.2::person_is_infected(X) :- person_contacted_Person(X, Y), person_is_infected(Y), vaccine_of_Person(X, b), person(X), person(Y).
```



Thank you

More info:

- https://cdmn.readthedocs.io/en/latest/pdmn.html
- https://gitlab.com/EAVISE/cdmn/pdmn
- Vandevelde, S., Verreet, V., De Raedt, L., & Vennekens, J. (2021). A tablebased representation for probabilistic logic: Preliminary results. ArXiv Preprint ArXiv:2110.01909.
- www.simonvandevelde.be

